

## Class 12 - Important Formulas

### Chapter 2 - Electric Potential and Capacitance

#### Electric Potential

S.No.	Term	Description
1	Electric Potential energy	<p><b>ΔU=-W</b></p> <p>Where <math>\Delta U</math> = Change in Potential energy and <math>W</math>= Work done by the electric lines of forces</p> <p>For a system of two particles</p> $U(r)=q_1 q_2 / 4\pi \epsilon r$ <p>where <math>r</math> is the separation between the charges.</p> <p>We assume <math>U</math> to be zero at infinity</p> <p>Similarly for a system of <math>n</math> charges</p> $U=\text{Sum of potential energy of all the distinct pairs in the system}$ <p>For example for three charges</p> $U=(1/4\pi\epsilon)(q_1 q_2 / r_{12} + q_2 q_3 / r_{23} + q_1 q_3 / r_{13})$
2	Electric PE of a charge	$=qV$ where $V$ is the potential there
3	Electric Potential	<p>Liken Electric field intensity is used to define the electric field; we can also use Electric Potential to define the field. Potential at any point <math>P</math> is equal to the work done per unit test charge by the external agent in moving the test charge from the reference point (without Change in KE)</p> $V_p=W_{ext}/q$ <p>So for a point charge</p> $V_p=Q/4\pi\epsilon r$ <p>where <math>r</math> is the distance of the point from charge</p>
4	Some points about Electric potential	<ol style="list-style-type: none"> <li>It is scalar quantity</li> <li>Potential at point due to system of charges will be obtained by the summation of potential of each charge at that point</li> <math display="block">V=V_1+V_2+V_3+V_4</math> <li>Electric forces are conservative force so work done by the electric force between two point is independent of the path taken</li> <li><math>V_2-V_1=-\int E \cdot dr</math></li> <li>In Cartesian coordinates system</li> <math display="block">dV=-E \cdot dr</math> <math display="block">dV=-(E_x dx + E_y dy + E_z dz)</math> <p>So <math>E_x=\partial V/\partial x</math>, <math>E_y=\partial V/\partial y</math> and <math>E_z=\partial V/\partial z</math></p> <p>Also</p> <math display="block">E=-[(\partial V/\partial x)i+(\partial V/\partial y)j+(\partial V/\partial z)k]</math> <li>Surface where electric potential is same everywhere is call equipotential surface</li> <li>Electric field components parallel to equipotential surface is always zero</li> </ol>
5	Electric dipole	<p>A combination of two charge <math>+q</math> and <math>-q</math> separated by the distance <math>d</math></p> $\mathbf{p}=qd$ <p>Where <math>d</math> is the vector joining negative to positive charge</p>
6	Electric potential due to dipole	$V=(1/4\pi\epsilon)(p \cos \theta / r^2)$ <p>where <math>r</math> is the distance from the center and <math>\theta</math> is angle made by the line from the axis of dipole</p>
7	Electric field due to dipole	$E_\theta=(1/4\pi\epsilon)(p \sin \theta / r^3)$ $E_r=(1/4\pi\epsilon)(2p \cos \theta / r^3)$ <p>Total <math>E=\sqrt{E_\theta^2+E_r^2}</math></p>

		$= (p/4\pi\epsilon r^3)(\sqrt{3\cos^2\theta + 1})$ Torque on dipole = $\mathbf{p} \times \mathbf{E}$ Potential Energy $U = -\mathbf{p} \cdot \mathbf{E}$
8	Few more points	1. $\int \mathbf{E} \cdot d\mathbf{l}$ over closed path is zero 2. Electric potential in the spherical charge conductor is $Q/4\pi\epsilon R$ where R is the radius of the shell and the potential is same everywhere in the conductor 3. Conductor surface is a equipotential surface

## Capacitance

S.No.	Term	Description
1	Capacitance C of the capacitor	$C = q/V$ or $q = CV$ -Unit of capacitance is Farads or $CV^{-1}$ capacitance of a capacitor is constant and depends on shape, size and separation of the two conductors and also on insulating medium being used for making capacitor.
2	Capacitance of parallel plate cap	$C = (\epsilon_0 A)/d$ where, $C$ = capacitance of capacitor $A$ = area of conducting plate $d$ = distance between plates of the capacitor $\epsilon_0 = 8.854 \times 10^{-12}$ and is known as electric permittivity in vacuum.
3	parallel plate air capacitor in presence of dielectric medium	$C = \epsilon A/d$
4	Capacitance of spherical capacitor having radii a, b ( $b > a$ )	(a) air as dielectric between them $C = (4\pi\epsilon_0 ab)/(b-a)$ (b) dielectric with relative permittivity $\epsilon$ $C = (4\pi\epsilon ab)/(b-a)$
5	Parallel combination of capacitors	$C = Q/V = C_1 + C_2 + C_3$ , resultant capacitance C is greater than the capacitance of greatest individual one.
6	Series combination of capacitors	$1/C = 1/C_1 + 1/C_2 + 1/C_3$ , resultant capacitance C is less than the capacitance of smallest individual capacitor.
7	Energy stored in capacitor	Energy stored in capacitor is $E = QV/2$ or $E = CV^2/2$ or $E = Q^2/2C$ factor 1/2 is due to average potential difference across the capacitor while it is charged.
8	Force between plates of capacitor	$F = \frac{Q}{2K\epsilon_0 A}$
9	Force per unit area of plates	$= \frac{\sigma^2}{2K\epsilon_0}$ Where $\sigma$ is charge per unit area.