

Class 12 - Important Formulas

Chapter 2 - Electric Potential and Capacitance

Electric Potential

S.No.	Term	Description
1	Electric Potential energy	$\Delta U = -W$ Where ΔU = Change in Potential energy and W = Work done by the electric lines of forces For a system of two particles $U(r) = q_1 q_2 / 4\pi\epsilon r$ where r is the separation between the charges. We assume U to be zero at infinity Similarly for a system of n charges U = Sum of potential energy of all the distinct pairs in the system For example for three charges $U = (1/4\pi\epsilon)(q_1 q_2 / r_{12} + q_2 q_3 / r_{23} + q_1 q_3 / r_{13})$
2	Electric PE of a charge	$= qV$ where V is the potential there
3	Electric Potential	Liken Electric field intensity is used to define the electric field; we can also use Electric Potential to define the field. Potential at any point P is equal to the work done per unit test charge by the external agent in moving the test charge from the reference point (without Change in KE) $V_p = W_{ext}/q$ So for a point charge $V_p = Q/4\pi\epsilon r$ where r is the distance of the point from charge
4	Some points about Electric potential	<ol style="list-style-type: none"> 1. It is scalar quantity 2. Potential at point due to system of charges will be obtained by the summation of potential of each charge at that point $V = V_1 + V_2 + V_3 + V_4$ 3. Electric forces are conservative force so work done by the electric force between two point is independent of the path taken 4. $V_2 - V_1 = -\int E \cdot dr$ 5. In Cartesian coordinates system $dV = -E \cdot dr$ $dV = -(E_x dx + E_y dy + E_z dz)$ So $E_x = \partial V / \partial x$, $E_y = \partial V / \partial y$ and $E_z = \partial V / \partial z$ Also $E = -[(\partial V / \partial x)i + (\partial V / \partial y)j + (\partial V / \partial z)k]$ 6. Surface where electric potential is same everywhere is call equipotential surface Electric field components parallel to equipotential surface is always zero
5	Electric dipole	A combination of two charge $+q$ and $-q$ separated by the distance d $p = qd$ Where d is the vector joining negative to positive charge
6	Electric potential due to dipole	$V = (1/4\pi\epsilon)(p \cos \theta / r^2)$ where r is the distance from the center and θ is angle made by the line from the axis of dipole
7	Electric field due to dipole	$E_\theta = (1/4\pi\epsilon)(p \sin \theta / r^3)$ $E_r = (1/4\pi\epsilon)(2p \cos \theta / r^3)$ Total $E = \sqrt{E_\theta^2 + E_r^2}$

		$= (p/4\pi\epsilon r^3)(\sqrt{3}\cos^2\theta + 1)$ <p>Torque on dipole = $\mathbf{p} \times \mathbf{E}$ Potential Energy $U = -\mathbf{p} \cdot \mathbf{E}$</p>
8	Few more points	1. $\oint \mathbf{E} \cdot d\mathbf{l}$ over closed path is zero 2. Electric potential in the spherical charge conductor is $Q/4\pi\epsilon R$ where R is the radius of the shell and the potential is same everywhere in the conductor 3. Conductor surface is a equipotential surface

Capacitance

S.No.	Term	Description
1	Capacitance C of the capacitor	$C = q/V$ or $q = CV$ -Unit of capacitance is Farads or CV^{-1} capacitance of a capacitor is constant and depends on shape, size and separation of the two conductors and also on insulating medium being used for making capacitor.
2	Capacitance of parallel plate cap	$C = (\epsilon_0 A)/d$ where, C = capacitance of capacitor A = area of conducting plate d = distance between plates of the capacitor $\epsilon_0 = 8.854 \times 10^{-12}$ and is known as electric permittivity in vacuum.
3	parallel plate air capacitor in presence of dielectric medium	$C = \epsilon A/d$
4	Capacitance of spherical capacitor having radii a, b ($b > a$)	(a) air as dielectric between them $C = (4\pi\epsilon_0 ab)/(b-a)$ (b) dielectric with relative permittivity ϵ $C = (4\pi\epsilon ab)/(b-a)$
5	Parallel combination of capacitors	$C = Q/V = C_1 + C_2 + C_3$, resultant capacitance C is greater then the capacitance of greatest individual one.
6	Series combination of capacitors	$1/C = 1/C_1 + 1/C_2 + 1/C_3$, resultant capacitance C is less then the capacitance of smallest individual capacitor.
7	Energy stored in capacitor	Energy stored in capacitor is $E = QV/2$ or $E = CV^2/2$ or $E = Q^2/2C$ factor 1/2 is due to average potential difference across the capacitor while it is charged.
8	Force between plates of capacitor	$F = \frac{Q^2}{2K\epsilon_0 A}$
9	Force per unit area of plates	$= \frac{\sigma^2}{2K\epsilon_0}$ Where σ is charge per unit area.